



# Neural Auction: End-to-End Learning of Auction Mechanisms for E-Commerce Advertising

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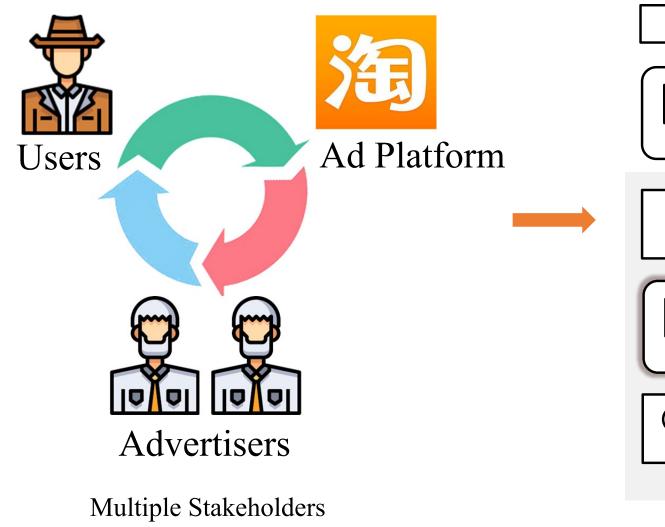


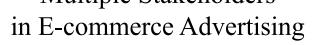


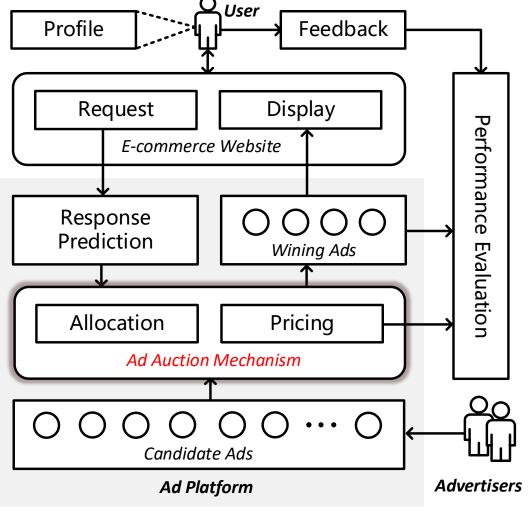
# Background



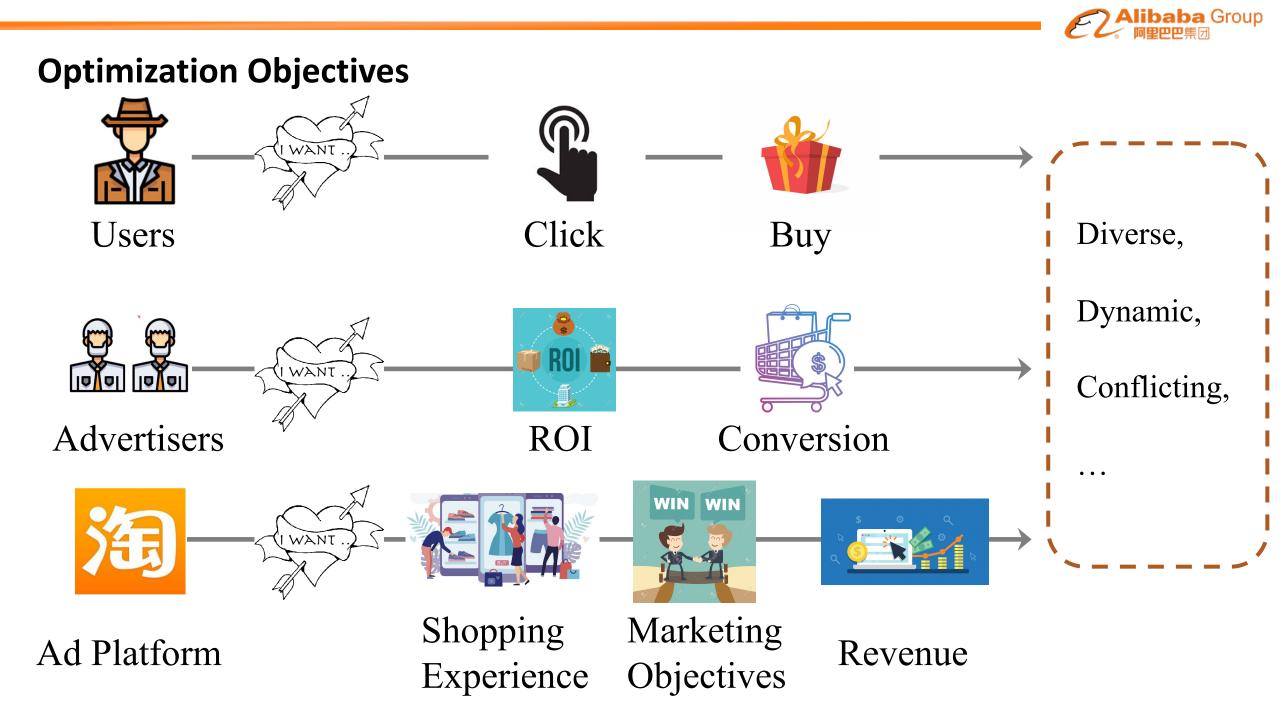
#### **Stakeholders in E-commerce Advertising**







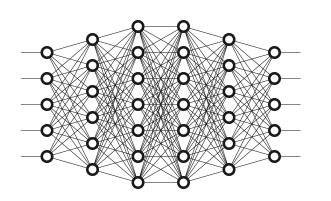
Ad Auction Mechanism





#### What do we focus on ?





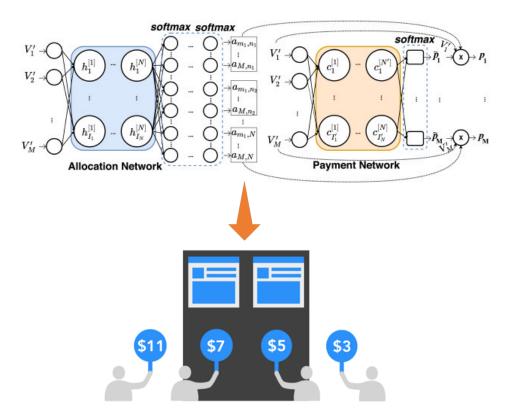
#### Auction Mechanism

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Myerson Auction Vickrey Auction Generalized Second-Price Auction

#### Deep Learning

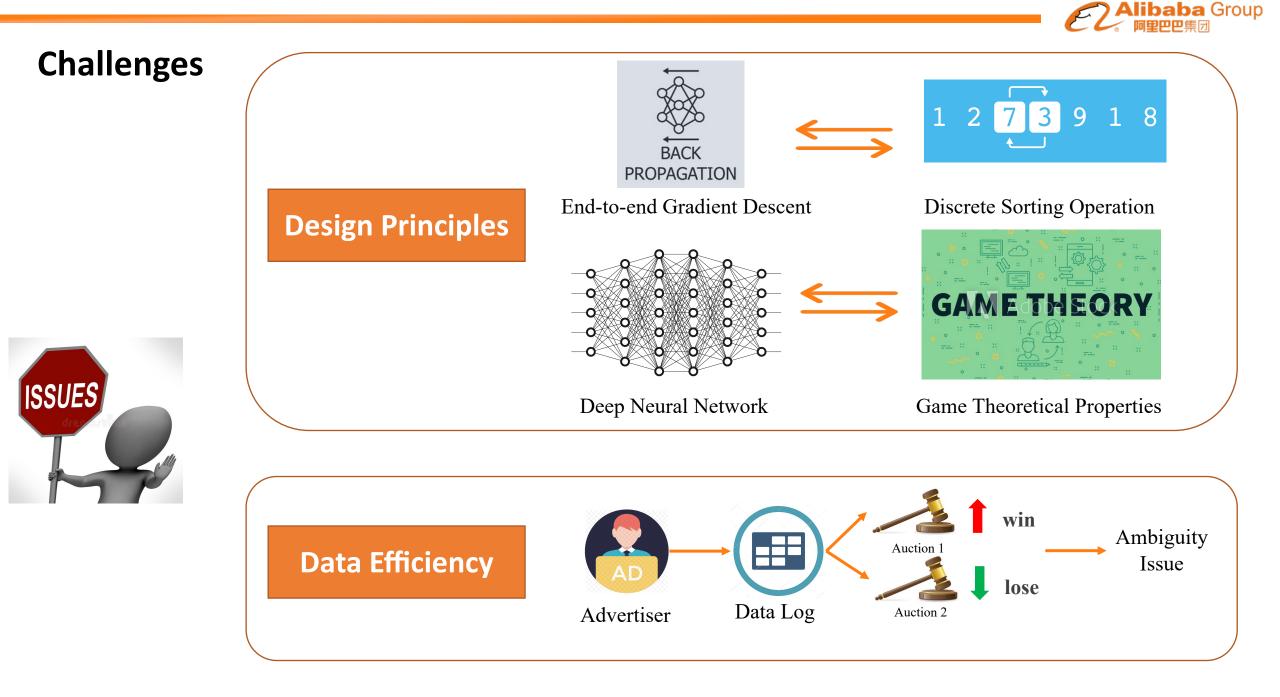
Deep Neural Network



#### Learning-based Mechanism Design

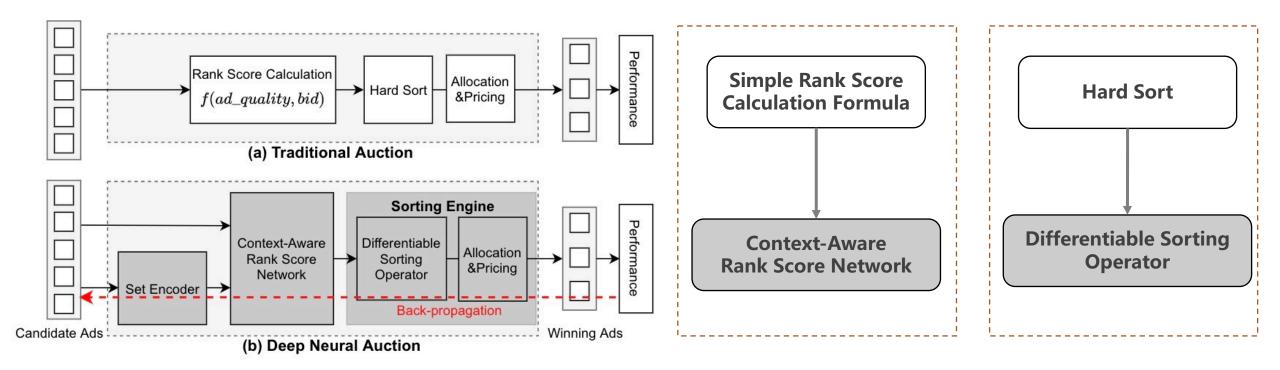
RegretNet [Dütting 19 ICML] ALGnet [Rahme 21 ICLR] DeepGSP [Zhang 21 WSDM]

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#### **Our Contribution :**

**Neural Auction**: making full use of the powerful deep learning on designing data-driven auction mechanisms for the industrial e-commerce advertising



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# **Problem Formulation**



### Formulation:

### Multiple performance metrics optimization in the competitive advertising environments

Mechanism:  $\mathcal{M}\langle \mathcal{R}, \mathcal{P} \rangle$  with allocation  $\mathcal{R}$  and pricing  $\mathcal{P}$ 

- • $\mathcal{R}$ : Select *K* ads from *N* candidates
- • $\mathcal{P}$ : Calculating payment on *K* wining ads

Goals:

- 1. Optimizing *L* performance metrics (RPM, CTR, CVR, GMV, etc.)
- 2. Desirable mechanism properties: IC & IR

$$\begin{array}{ll} \underset{\mathcal{M}}{\text{maximize}} & \mathbb{E}_{\mathbf{b}\sim\mathcal{D}}\left[\sum_{j=1}^{L}w_{j}\times f_{j}(\mathbf{b};\mathcal{M})\right]\\ \text{s.t.} & Incentive \ compatibility \ (IC) \ constraint, \end{array}$$

Individual Rationality (IR) constraint,



### **Formulation:**

- Second-Price Auctions:
  - Nice interpretability
  - Easy to deploy in industry
  - The score reflects the degree of ad quality
- Learning-based Second-Price Auction Framework:
  - Deep neural network based rank score function:  $r_i(b_i)$
  - The training of this non-linear model is under the guideline of optimization objective
- Allocation Scheme  $\mathcal{R}$ :  $r_1(b_1) \ge r_2(b_2) \ge \cdots \ge r_N(b_N)$
- Payment Rule  $\mathcal{P}$ :  $p_i = r_i^{-1}(r_{i+1}(b_{i+1}))$





### **Economic Properties**

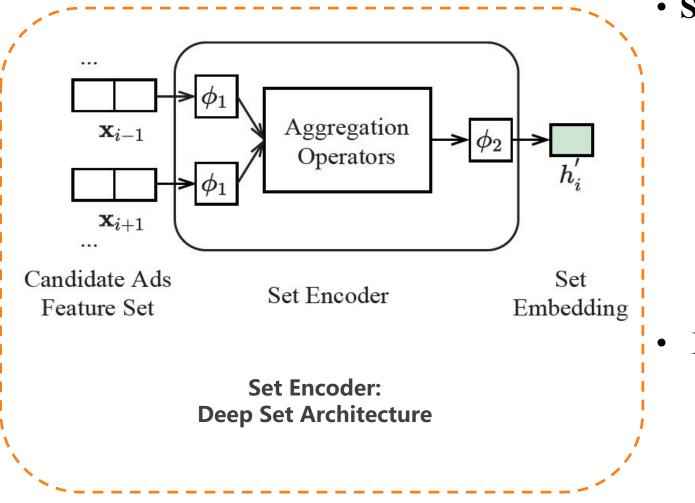
- Game Theoretical Property of Auction Mechanism:
  - Incentive Compatibility (IC): truthfully report the bid
  - Individual Rationality (IR): would not be charged more than their maximum willing-to-pay
- Value Maximizer:
  - A value maximizer *i* optimizes value  $v_i$  while keeping payment  $p_i$  below her maximum willing-to-pay  $m_i$ ; when value is equal, a lower  $p_i$  is preferred.
  - "Value maximizer" has been widely adopted in industry, such as Yahoo! and Google.
- IC & IR conditions for Value Maximizers:
  - Monotonicity: An advertiser would win the same or a higher slot if she reports a higher bid;
  - **Critical price**: The payment for the winning advertiser is the minimum bid that she needs to report to maintain the same slot.



# **Our Approach: Neural Auction**



#### **Neural Auction -- Auction Context Encoding**



#### Set Encoder:

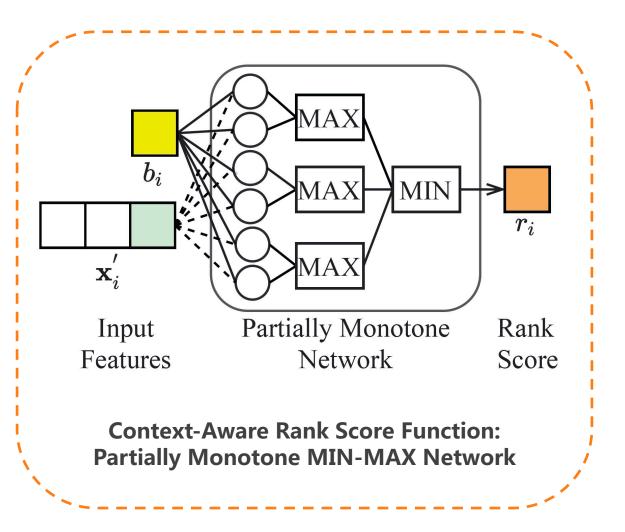
- Automatically extract the feature of the auction context from all the candidate ads via DeepSet [17 Nips].
- Attached as an augmented feature for each ad to overcome the ambiguity issue.

DeepSet Aggregation:

 $h_i = \sigma(\phi_1(\mathbf{x}_i))$ 

 $h'_i = \sigma(\phi_2(\operatorname{avgpool}(\mathbf{h}_{-i})))$ 

#### **Neural Auction -- Context-Aware Rank Score**



#### Partially Monotone MIN-MAX Network

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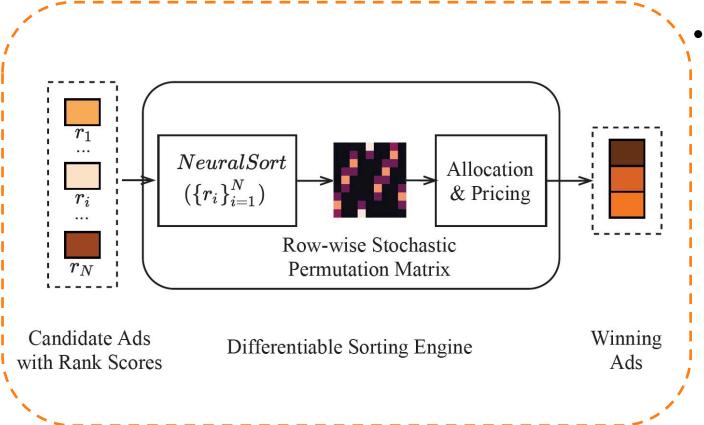
- Strictly non-decreasing on bid
- The inverse transform can be directly obtained.

#### • Rank Score:

- $r_i = \min_{q \in [Q]} \max_{z \in [Z]} (e^{w_{qz}} \times b_i + w'_{qz} \times \mathbf{x}'_i + \alpha_{qz})$
- Payment:

$$p_i = \max_{z \in [Z]} \min_{q \in [Q]} e^{-w_{qz}} (r_{i+1} - \alpha_{qz} - w'_{qz} \times \mathbf{x}'_i)$$

#### **Neural Auction -- Differentiable Sorting Engine**



### • Neural Sort [ICLR19]:

• A continuous relaxation to the sorting operator.

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• Enabling gradient-based stochastic optimization over the allocation & pricing results.

$$M_{r}[k,i] = \begin{cases} 1 & \text{if } i = \arg\max(c_{k}), \\ 0 & \text{otherwise,} \end{cases}$$
$$\hat{M}_{r}[k,:] = \operatorname{softmax}(\frac{c_{k}}{\tau}),$$



#### **Neural Auction -- Model Training**

• Loss Function:

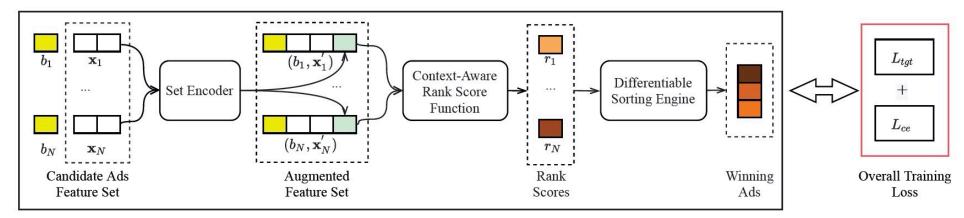
 $\mathcal{L}_{tgt}$  : Minimizing the sum of top-K expected negated performance metrics:

$$\mathcal{L}_{tgt} = -\sum_{i=1}^{K} \hat{M}_{r}[i,:] \cdot F_{all}$$
$$F_{all} = \left[\sum_{l=1}^{L} \lambda_{l} \times f_{l}^{1}, \cdots, \sum_{l=1}^{L} \lambda_{l} \times f_{l}^{N}\right]^{T}$$

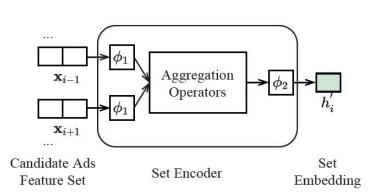
 $\mathcal{L}_{ce}$  : Minimizing the permutation prediction error:

$$\mathcal{L}_{ce} = -\frac{1}{N} \sum_{k=1}^{N} \sum_{i=1}^{N} \mathbb{1}(M_{y}[k,i] = 1) \log \hat{M}_{r}[k,i]$$

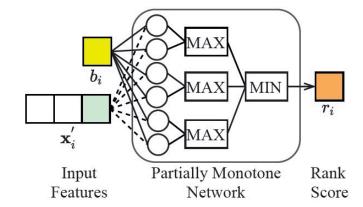
#### **Neural Auction -- Overall Framework**



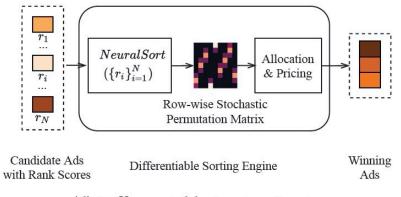
(a) Deep Neural Auction Architecture



(b) Set Encoder: Deep Set Architecture



(c) Context-Aware Rank Score Function: Partially Monotone MIN-MAX Network



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(d) Differentiable Sorting Engine: NeuralSort Module



# **Experiments**

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#### **Offline Experiments**

- Data Set: 5870k records logged data from Taobao.
- Baselines: GSP, uGSP, DeepGSP [WSDM 21]
- Performance metrics: RPM, CTR, CVR, GMV
- Intuitive comparisons:  $\lambda \times RPM + (1 \lambda) \times X$

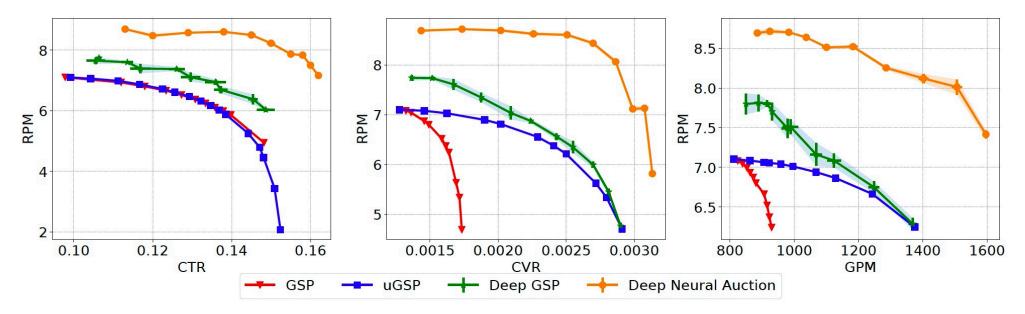
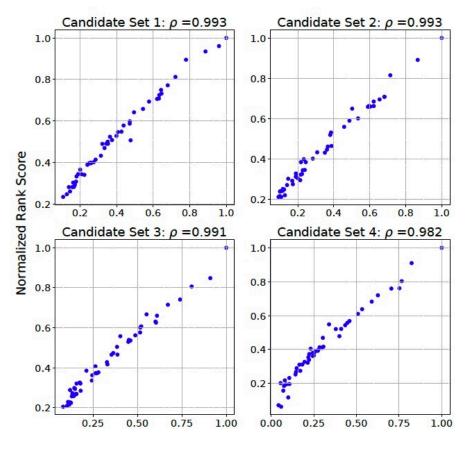


Figure 4: The performance of DNA and other baseline mechanisms in the offline experiments.



#### **Offline Experiments**



Normalized Targeted Performance Metrics

Figure 3: The positive correlations between learned rank scores and the targeted performance metrics. Each blue dot represents an ad in the candidate set. • Interpretability:

- The strong positive correlation between the learned rank scores and the performance metrics.
- Implicitly guide advertisers to improve ad quality and then the rank score.



### **Offline Experiments**

## • Data-driven IC Metric for Value Maximizers

•  $\Psi_{v}$ : regret on value

$$\Psi_{v} = \frac{1}{N} \sum_{i=1}^{N} \frac{1}{\beta_{k_{i}}} \max_{b'_{i}} ((\beta_{k'_{i}} - \beta_{k_{i}}) \times \mathbb{1}(p_{i}(b'_{i}) < m_{i})),$$

•  $\Psi_p$ : regret on payment

 $\Psi_p = \frac{1}{N} \sum_{i=1}^N \frac{1}{\beta_{k_i} p_i(b_i)} \max_{b'_i} ((\beta_{k_i} p_i(b_i) - \beta_{k'_i} p_i(b'_i)) \times \mathbb{1}(k'_i = k_i))$ 

Table 1: IC Metric ( $\Psi$ ) experiments under four tasks with 1000 PV requests randomly selected from the test data. For each bidder, we randomly generate 100 perturbations (ranging from 0.0 to 2.0 times) to her value.

	DNA		uGFP	
	$\Psi_v$	$\Psi_p$	$\Psi_v$	$\Psi_p$
1.0×RPM	0	0.042%	0	13.312%
0.5×RPM+0.5×CTR	0	0.059%	0	21.616%
0.5×RPM+0.5×CVR	0	0.118%	0	19.280%
0.5×RPM+0.5×GPM	0	0.028%	0	16.400%



#### **Online Experiments**

- Online A/B tests:
  - 1% of whole production traffic
  - 20210125 20210208 (about one billion auctions).

Table 2: Online A/B test compared with uGSP on promoting different performance metrics, keeping the same RPM level.

% Improved	Deep GSP	DNA
CTR	+6.43%	+11.58%
CVR	+6.38%	+31.26%
GPM	+2.77%	+16.17%

Table 3: Online A/B test (nearly two months) compared with GSP on promoting all performance metrics.

	RPM	CTR	CVR	GPM
% Improved	+5.68%	+18.93%	+14.68%	+14.53%



# Conclusion

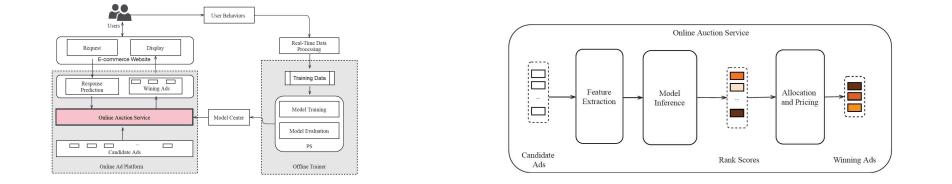


#### Conclusions

 ✓ We have proposed a Deep Neural Auction mechanism, towards learning data efficient and end-to-end auction mechanisms with the guarantee of game theoretical property for e-commerce advertising.

✓ Both offline and online experimental results on a real-world e-commerce ad platform validate the effectiveness of the proposed auction mechanism.

### Deployment details: https://arxiv.org/abs/2106.03593



We hope the insights and lessons obtained from our industrial deployment would motivate and encourage researchers working on learning-based auction design in both theory and practice.





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